Reconciling Gross Output TFP Growth with Value Added TFP Growth

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ABSTRACT
This article obtains relatively simple exact expressions that relate value added total factor productivity growth (TFP) in a value added framework to the corresponding measures of TFP growth in a gross output framework when Laspeyres or Paasche indexes are used to aggregate outputs and inputs. Basically, as the input base becomes smaller, the corresponding estimates of TFP growth become larger. A fairly simple approximate relationship between Fisher indexes of gross output TFP growth and the corresponding Fisher index of value added TFP growth is also derived. The methodology developed in this article has a number of applications.

SCHREYER (2001:26) DEVELOPED AN approximate formula to relate total factor productivity growth (or multifactor productivity growth) in a gross output model of production to TFP (or MFP) growth in a value added setting. In this article, we take another look at this issue and develop an exact relationship between the two measures when Laspeyres (or Paasche) output and input indexes are used to compute aggregate growth rates of inputs and outputs. We develop rules relating the two productivity concepts that are simpler than the existing rules that have been developed in the literature.

Sections 1 and 2 discuss the construction of the aggregate outputs and inputs using the Laspeyres and Paasche formulae respectively, while Section 3 uses the Fisher (1922) ideal index number formula to aggregate inputs and outputs. Section 4 concludes.

The Laspeyres Case
We first consider the situation where Laspeyres indexes are used to aggregate outputs and inputs. For simplicity, consider a situation where we want to compute gross output and value added productivity growth rates for a production unit that produces gross output $q_Y^t > 0$ at prices $p_Y^t > 0$, uses intermediate input $q_M^t > 0$ at prices $p_M^t > 0$ and uses primary input $q_X^t > 0$ at prices $p_X^t > 0$ for $t = 0, 1$.

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2 See Balk (2009) for a comprehensive discussion on this topic. We obtain approximately the same result as Balk obtains but our method of derivation is much simpler.

3 In the case where there are many inputs and outputs, the output and input quantity ratio aggregates, $q_Y^t > 0 / q_Y^0 > 0$, $q_M^t > 0 / q_M^0 > 0$ and $q_X^t > 0 / q_X^0 > 0$ the output and input quantity ratio aggregates can be interpreted as Laspeyres indexes of the micro quantities. The corresponding aggregate price ratios are of course Paasche price indexes.
Define the period \( t \) value of gross output as \( v_Y^t = p_Y^t \cdot q_Y^t \) for \( t = 0,1 \), while intermediate inputs and primary inputs are defined as \( v_M^t = p_M^t \cdot q_M^t \), and \( v_X^t = p_X^t \cdot q_X^t \). Define (one plus) the growth rates of output, intermediate inputs and primary inputs as \( \Gamma_Y, \Gamma_M \) and \( \Gamma_X \) as follows:

\[
(1) \quad \Gamma_Y = q_Y^1 / q_Y^0 \quad ; \quad \Gamma_M = q_M^1 / q_M^0 \quad \text{and} \quad \Gamma_X = q_X^1 / q_X^0 .
\]

We assume that the value of inputs equals the value of outputs in period 0:

\[
(2) \quad v_Y^0 = v_M^0 + v_X^0 .
\]

(One plus) gross output TFP growth using Laspeyres quantity indexes, \( \Pi_G \), is defined as follows:

\[
(3) \quad \Pi_G \equiv \Gamma_Y / [s_M^0 \Gamma_M + s_X^0 \Gamma_X]
\]

where the period 0 input cost shares \( s_M^0 \) and \( s_X^0 \) are defined as follows:

\[
(4) \quad s_M^0 = v_M^0 / [v_M^0 + v_X^0 ] \quad \text{using (2)};
\]

\[
= v_M^0 / v_Y^0 \quad \text{using (2)};
\]

\[
(5) \quad s_X^0 = v_X^0 / [v_M^0 + v_X^0 ] \quad \text{using (4)};
\]

\[
= 1 - s_M^0 .
\]

We now need to define value added TFP growth. We use the Laspeyres index number formula to construct an aggregate of gross output less intermediate input. We assume that the quantities of gross output and intermediate input are positive but we change the sign of the price of intermediate inputs from a positive sign to a negative sign in order to construct a Laspeyres index of real value added. Thus (one plus) real value added TFP growth using a Laspeyres quantity index to construct real value added growth, \( \Pi_{VA} \), is defined as follows:

\[
(6) \quad \Pi_{VA} \equiv \frac{[s_Y^0 \Gamma_Y + s_M^0 \Gamma_M]}{\Gamma_X} ,
\]

where the period 0 value added output cost shares \( s_Y^0 \) and \( s_M^0 \) are defined as follows:

\[
(7) \quad s_Y^0 \equiv \frac{v_Y^0}{[v_Y^0 - v_M^0 ]} = 1 / [1 - (v_M^0 / v_Y^0 )] \quad \text{using (4)};
\]

\[
(8) \quad s_M^0 \equiv -v_M^0 / [v_Y^0 - v_M^0 ] = 1 - s_Y^0 = -s_M^0 / [1 - s_M^0 ] \quad \text{using (7)};
\]

Now substitute (7) and (8) into (6) and we obtain the following expression for (one plus) value added TFP growth:

\[
(9) \quad \Pi_{VA} \equiv \frac{\Gamma_Y - s_M^0 \Gamma_M}{(1 - s_M^0 )\Gamma_X} .
\]

We can also substitute (5) into (3) and obtain the following expression for (one plus) gross output TFP growth:

\[
(10) \quad \Pi_G \equiv \Gamma_Y / [s_M^0 \Gamma_M + (1 - s_M^0 )\Gamma_X] .
\]

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4 The capital gamma is called a growth factor.

5 Note that \( s_M^0 \Gamma_M + s_X^0 \Gamma_X \) is the Laspeyres quantity index of all inputs.

6 These shares sum to one but of course \( s_M^0 \) is negative and so the “share” will not be bounded from below by 0 and above by 1.

7 Note that we did not change the sign of \( v_Y^0 > 0 \) and \( s_M^0 > 0 \). Thus, using (7), \( s_M^0 < 0 \). We assume that period 0 nominal value added, \( v_Y^0 - v_M^0 \), is greater than 0.
Comparing (9) and (10), it can be seen that both value added and gross output TFP (one plus) growth rates can be expressed in terms of (one plus) the growth rates of output, intermediate input and primary input (Γ₀, G and Γχ) and the share of intermediate input in total input, s₀.

Now define the rate of gross output TFP growth as πG equal to ΠG less 1 and the rate of real value added TFP growth as πVA equal to ΠVA less 1. We can obtain the following alternative expressions for πG and πVA:

\[
(11) \quad \pi_G = \Pi_G - 1 = (\Gamma_Y / [s_0^0 \Gamma_M + (1 - s_0^0) \Gamma_X]) - 1 = [\Gamma_Y - s_0^0 \Gamma_M - (1 - s_0^0) \Gamma_X] / [s_0^0 \Gamma_M + (1 - s_0^0) \Gamma_X] \quad \text{using (10)}.
\]

\[
(12) \quad \pi_{VA} = \Pi_{VA} - 1 = (\Gamma_Y / [s_0^0 \Gamma_M - (1 - s_0^0) \Gamma_X]) - 1 = [\Gamma_Y - s_0^0 \Gamma_M - (1 - s_0^0) \Gamma_X] / [(1 - s_0^0) \Gamma_X] \quad \text{using (9)}.
\]

When we construct the ratio of value added TFP growth to gross output TFP growth and we obtain the following exact formula relating the two productivity concepts:

\[
(13) \quad \pi_{VA} / \pi_G = (1 - s_0^0)^{-1} (s_0^0 \Gamma_M + (1 - s_0^0) \Gamma_X) = (s_X^0)^{-1} [s_M^0 \Gamma_M + (1 - s_M^0) \Gamma_X] / \Gamma_X \quad \text{using (5)}.
\]

\[
= (s_Y^0)^{-1} [s_M^0 \Gamma_M + (1 - s_M^0) \Gamma_X] / \Gamma_X \quad \text{using (2) and (5)}.
\]

Thus the larger is the share of intermediate inputs in total period 0 input, s₀, the larger will be (1 - s₀)⁻¹ and hence, the greater will be value added TFP growth relative to gross output TFP growth. Similarly, the larger is (one plus) aggregate input growth s₀¹ Γ₀ + (1 - s₀)Γ₀ over the two periods being compared relative to (one plus) primary input growth Γ₀, the larger will be value added TFP growth relative to gross output TFP growth. Typically, (one plus) aggregate input growth will not be all that different from (one plus) primary input growth (both terms will be close to unity) so the term (1 - s₀)⁻¹ = 1/s₀⁻¹ = v₀⁻¹/ν₀⁻¹ will explain almost all of the difference in the two TFP growth rates.

Note that the last equation in (13) shows that πVA/πG is approximately equal to ν₀⁻¹/ν₀⁻¹, the value of gross output, ν₀⁻¹, divided by the value of primary inputs, ν₀⁻¹, which in turn is equal to value added, ν₀⁻¹ - ν₀⁻¹, using our assumption (2). The ratio of gross output to value added is frequently called the Domar factor (Balk, 2009:249).

The above results can readily be generalized to many outputs and inputs due to the consistency in aggregation properties of the Laspeyres formula.

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8 We need to assume that ΠG ≠ 0.

9 Note that 1 - s₀ is equal to s₀, the share of primary inputs in total inputs used in period 0. The first equation in (12) is roughly equivalent to Domar’s (1961:725) equation (4.6) while the third equation in (12) is roughly equivalent to Balk’s (2009:248) equation (20).

10 Thus if (Laspeyres) gross output TFP growth πG is 0.5 per cent and the period 0 primary input share of total input s₀ is 1/2, then (Laspeyres) value added TFP growth πVA will be approximately (s₀⁻¹)(0.5%) = 1.0% if s₀ = 1/3, then πVA = (1/3)⁻¹(0.5%) = 1.5%.
The Paasche Case

We now consider the situation where Paasche indexes are used to aggregate outputs and inputs. Again, define (one plus) the growth rates of output, intermediate inputs and primary inputs as \( \Gamma_y \), \( \Gamma_M \) and \( \Gamma_X \) by equations (1) when we are dealing with multiple outputs and inputs, these ratios are to be interpreted as being equal to Paasche indexes of gross output, intermediate inputs and primary inputs. We assume that the value of inputs equals the value of outputs in period 1:

\[ v_y^1 = v_M^1 + v_X^1 \]  

(One plus) gross output TFP growth using Paasche quantity indexes, \( \Pi^*_G \), is defined as follows:

\[ \Pi^*_G = \frac{\Gamma_y^1}{r^1 + \Gamma_X^1 - 1} \]  

where the period 0 input cost shares \( s_M^1 \) and \( s_X^1 \) are defined as follows:

\[ s_M^1 \equiv \frac{v_M^1}{v_y^1 + v_X^1} \]  
\[ s_X^1 \equiv \frac{v_X^1}{v_y^1 + v_X^1} \]  

We now need to define Paasche value added TFP growth. We use the Paasche index number formula to construct an aggregate of gross output less intermediate input. We assume that the quantities of gross output and intermediate input are positive but we change the sign of the price of intermediate inputs from a positive sign to a negative sign in order to form a Paasche index of real value added. Thus (one plus) real value added TFP growth using a Paasche quantity index to construct real value added growth, \( \Pi^*_VA \), is defined as follows:

\[ \Pi^*_VA \equiv \frac{\Gamma_y^1 \Gamma_M^{-1} + s_M^1 \Gamma_X^{-1}^{-1}}{\Gamma_X} \]  

where the period 1 value added output expenditure shares, \( S_y^1 \) and \( S_M^1 \), are defined as follows:

\[ S_y^1 \equiv \frac{1}{1 - (v_M^1 / v_y^1)} \]  
\[ S_M^1 \equiv \frac{1 - S_y^1}{1 - S_M^1} \]  

Now substitute (19) and (20) into (18) and we obtain the following expression for (one plus) value added Paasche TFP growth:

\[ \Pi^*_VA \equiv \frac{\Gamma_y^1 \Gamma_M^{-1} + s_M^1 \Gamma_X^{-1}^{-1}}{\Gamma_X} \]
We can also substitute (17) into (15) and obtain the following expression for (one plus) gross output Paasche TFP growth:

\[
(22) \quad \Pi_G^* = \frac{\Gamma_Y}{[s_M^1 \Gamma_M^{-1} + (1 - s_M^1) \Gamma_X^{-1}]} - 1
\]

\[
= [s_M^1 \Gamma_M^{-1} + (1 - s_M^1) \Gamma_X^{-1}] / \Gamma_Y
\]

Comparing (21) and (22), it can be seen that both value added and gross output Paasche TFP (one plus) growth rates can be expressed in terms of (one plus) the growth rates of (Paasche) output, intermediate input and primary input \((\Gamma_Y, \Gamma_M \text{ and } \Gamma_X)\) and the period 1 share of intermediate input in total input, \(s_M^1\).

Now compute \((\Pi_{VA}^*)^{-1} - 1\) and \((\Pi_G^*)^{-1} - 1\) using (21) and (22):

\[
(23) \quad (\Pi_{VA}^*)^{-1} - 1 = \left\{ [\Gamma_Y^{-1} - s_M^1 \Gamma_M^{-1}] / (1 - s_M^1) \Gamma_X^{-1} \right\} - 1
\]

\[
= [\Gamma_Y^{-1} - s_M^1 \Gamma_M^{-1} - (1 - s_M^1) \Gamma_X^{-1}] / (1 - s_M^1) \Gamma_X^{-1}
\]

\[
(24) \quad (\Pi_G^*)^{-1} - 1 = \left\{ \frac{\Gamma_Y^{-1}}{s_M^1 \Gamma_M^{-1} + (1 - s_M^1) \Gamma_X^{-1}} \right\} - 1
\]

\[
= [\Gamma_Y^{-1} - s_M^1 \Gamma_M^{-1} - (1 - s_M^1) \Gamma_X^{-1} / s_M^1 \Gamma_M^{-1} + (1 - s_M^1) \Gamma_X^{-1}]
\]

Now take the ratio of (23) and (24) and we obtain the following identity:\(^{15}\)

\[
(25) \quad [(\Pi_{VA}^*)^{-1} - 1] / [(\Pi_G^*)^{-1} - 1] = \\
\frac{[s_M^1 \Gamma_M^{-1} + (1 - s_M^1) \Gamma_X^{-1}]}{1 - s_M^1 [s_M^1 \Gamma_M^{-1} + (1 - s_M^1) \Gamma_X^{-1}] / \Gamma_Y}
\]

Define the Paasche rate of gross output TFP growth as \(\pi_G^*\) equal to \(\Pi_G^*\) less 1 and the Paasche rate of real value added TFP growth as \(\pi_{VA}^*\) equal to \(\Pi_{VA}^*\) less 1:

\[
(26) \quad \pi_G^* = \Pi_G^* - 1
\]

\[
(27) \quad \pi_{VA}^* = \Pi_{VA}^* - 1
\]

Now multiply both sides of (25) by \(\Pi_{VA}^*/\Pi_G^*\) and we obtain the following equation:

\[
(28) \quad \pi_{VA}^*/\pi_G^* = \left\{ [\Pi_{VA}^*/\Pi_G^*] \left\{ [s_M^1 \Gamma_M^{-1} - (1 - s_M^1) \Gamma_X^{-1}] / (1 - s_M^1) \Gamma_X^{-1} \right\} \right\}
\]

\[
\quad \left\{ [\Pi_{VA}^*/\Pi_G^*] \left\{ [s_M^1 \Gamma_M^{-1} + (1 - s_M^1) \Gamma_X^{-1}] / \Gamma_Y \right\} \right\}
\]

\[
= (1 - s_M^1) [s_M^1 \Gamma_M^{-1} + s_M^1 \Gamma_M^{-1}] / \Gamma_Y
\]

\[
= (s_M^1)^{-1} [s_M^1 \Gamma_M^{-1} / (1 - s_M^1) \Gamma_X^{-1}]
\]

\[
= (s_M^1)^{-1} \left\{ [s_M^1 \Gamma_M^{-1} + s_M^1 \Gamma_M^{-1}] / \Gamma_Y \right\}
\]

\[
= (s_M^1)^{-1} \left\{ [s_M^1 \Gamma_M^{-1} + s_M^1 \Gamma_M^{-1}] / \Gamma_Y \right\}
\]

\[
= (s_M^1)^{-1} \left\{ [s_M^1 \Gamma_M^{-1} + s_M^1 \Gamma_M^{-1}] / \Gamma_Y \right\}
\]

Thus the larger is the share of intermediate inputs in total period 1 input, \(s_M^1\), the larger will be \((1 - s_M^1)\) and hence the larger will be value added Paasche TFP growth relative to

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\(^{15}\) We need to assume that \((\Pi_G^*)^{-1} - 1 \neq 0\) which will imply that \(\pi_G^* = \Pi_G^* - 1\) is also not equal to 0 since \(\Pi_G^* > 0\).
Paasche gross output TFP growth. Of course, 
\((1 - s_M^{-1})^{-1}\) is equal to \(1/sX^1\) which in turn is equal to the period 1 Domar augmentation factor, \(v_Y^1/v_X^1\), which in turn is equal to the period 1 value of gross output divided by the period 1 value of primary input.16 Similarly, the larger is (one plus) real value added growth \([s_Y^1 \Gamma_Y^{-1} + s_M^1 \Gamma_M^{-1}]^{-1}\) over the two periods being compared relative to (one plus) gross output growth \(\Gamma_Y\),17 the larger will be Paasche value added TFP growth relative to Paasche gross output TFP growth. Note the similarity of Paasche formula (28) to our earlier Laspeyres formula (13). Typically, (one plus) real value added growth will not be all that different from (one plus) gross output growth (both terms will be close to unity) so the Paasche Augmentation Factor \(1 - s_M^{-1}\) will explain almost all of the difference in the two Paasche TFP growth rates.

The above results can readily be generalized to many outputs and inputs due to the consistency in aggregation properties of the Paasche formula.

The Fisher Case

(One plus) the Fisher (1922) index of value added productivity growth, \(\Pi_{VA}^F\), is defined as the geometric mean of the corresponding Laspeyres and Paasche measures of (one plus) value added TFP growth, \(\Pi_{VA}\) and \(\Pi_{VA}^*\):

\[
(29) \quad \Pi_{VA}^F = [\Pi_{VA} \cdot \Pi_{VA}^*]^{1/2}
\]

Similarly, (one plus) the Fisher (1922) index of gross output, \(\Pi_{G}^F\), is defined as the geometric mean of the corresponding Laspeyres and Paasche measures of (one plus) gross output TFP, \(\Pi_{G}\) and \(\Pi_{G}^*\):

\[
(30) \quad \Pi_{G}^F = [\Pi_{G} \cdot \Pi_{G}^*]^{1/2}
\]

Finally, define the Fisher (1922) indexes of value added and gross output productivity growth, \(\pi_{VA}^F\) and \(\pi_{G}^F\), as follows:

\[
(31) \quad \pi_{VA}^F = \Pi_{VA}^F - 1
\]

\[
(32) \quad \pi_{G}^F = \Pi_{G}^F - 1
\]

Equations (9) and (10) give exact expressions for the Laspeyres indexes of \(\Pi_{VA}\) and \(\Pi_{G}\), while equations (21) and (22) give exact expressions for the Paasche indexes of \(\Pi_{VA}^*\) and \(\Pi_{G}^*\). Hence we could use these expressions to calculate the Fisher variables (29)-(32) and we would end up with an exact expression for the ratio of Fisher index value added TFP growth to Fisher gross output growth \(\pi_{VA}^F/\pi_{G}^F\). However, the resulting expression is difficult to interpret and so we will resort to a different strategy that makes use of equations (13) and (28) as the constants \(\gamma\) and \(\gamma^*\):19

\[
(33) \quad \frac{\pi_{VA}}{\pi_{G}} = \frac{(s_X^0)^{-1} - s_M^0 \Gamma_M^0 + (1 - s_M^0) \Gamma_X^0)}{\Gamma_X^0} = \gamma
\]

16 Assumption (14) ensures that \(v_Y^1/v_X^1 > 1\).
17 Note that \([s_Y^1 \Gamma_Y^{-1} + s_M^1 \Gamma_M^{-1}]^{-1}\) is the Paasche index of real value added growth and \(\Gamma_Y\) is to be interpreted as the Paasche index of gross output growth if there are many outputs and we are aggregating outputs in two stages using the Paasche formula.
18 These approximations will typically be very close.
19 These constants can be regarded as magnification factors; they magnify the gross output TFP growth rates into the corresponding real value added TFP growth rates.
Using definitions (11), (12), (26) and (27), equations (33) and (34) imply the following relations:

\[(35)\]  
\[\pi_{VA}^* = \gamma (\Pi^*_G - 1)\]

\[(36)\]  
\[\pi_{VA}^* - 1 = \gamma^* (\Pi^*_G - 1)\]

Using definitions (29) and (31), we have the following equations:

\[(37)\]  
\[\pi_{VA}^F = [\pi_{VA} \cdot \pi_{VA}^*]^{1/2} - 1\]

\[= (1/2)\pi_{VA} + (1/2)\pi_{VA}^* - 1\]

where we have approximated the geometric mean by an arithmetic mean:

\[= (1/2)[\Pi_{VA} - 1] + (1/2)[\Pi_{VA}^* - 1]\]

\[= (1/2)\gamma [\Pi^*_G - 1] + (1/2)\gamma^* [\Pi^*_G - 1]\]

where the last equation follows using (35) and (36). Using definitions (30) and (32), we have the following equations:

\[(38)\]  
\[\pi_{G}^F = [\Pi_G \cdot \Pi_G^*]^{1/2} - 1\]

\[= (1/2)\Pi_G + (1/2)\Pi_G^* - 1\]

where we have approximated the geometric mean by an arithmetic mean

\[= (1/2)[\Pi_G - 1] + (1/2)[\Pi_G^* - 1]\]

If \((1/2)[\Pi_G - 1] + (1/2)[\Pi_G^* - 1]\) is not equal to zero, we can take the ratio of \(\pi_{VA}^F\) to \(\pi_{G}^F\) and using (37) and (38), we obtain the following approximate relationship of Fisher value added TFP growth to Fisher gross output TFP growth:

\[(39)\]  
\[\pi_{VA}^F / \pi_{G}^F = \left\{ \gamma [\Pi^*_G - 1] + \gamma^* [\Pi^*_G - 1] \right\} / \left\{ [\Pi_G - 1] + [\Pi^*_G - 1] \right\}\

\[= w\gamma + (1 - w)\gamma^*\]

where

\[w = [\Pi_G - 1] / \left\{ [\Pi_G - 1] + [\Pi^*_G - 1] \right\}.\]

Thus \(\pi_{VA}^F / \pi_{G}^F\) is approximately equal to a weighted average of the Laspeyres and Paasche magnification factors, \(\gamma\) and \(\gamma^*\).

If we are willing to make a further approximation that the Laspeyres and Paasche indexes of gross output growth are approximately equal so that \(\Pi_G = \Pi^*_G\), then we obtain the following very simple approximate relationship between Fisher value added TFP growth and Fisher gross output TFP growth:

\[(40)\]  
\[\pi_{VA}^F / \pi_{G}^F = (1/2)\gamma + (1/2)\gamma^*\]

**Conclusion**

We have obtained relatively simple exact expressions for the relationship between the rate of gross output TFP growth and the corresponding rate of real value added TFP growth when the Laspeyres or Paasche index number formulae are used to aggregate inputs and outputs. We also obtained a simple approximate expression relating value added TFP growth to gross output TFP growth.

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20 The weights for \(\gamma\) and \(\gamma^*\) will sum to unity but they need not be nonnegative unless \(\Pi_G - 1\) and \(\Pi^*_G - 1\) have the same sign. This will almost always be the case empirically.
when the Fisher formula is used to aggregate inputs and outputs. Generally speaking, gross output TFP growth is magnified when we move to value added TFP growth and the magnification factor is approximately equal to the reciprocal of the share of primary inputs in total input use.

The same methodology can be used in other situations. For example, we may want to compare value added productivity growth to net value added productivity growth where the latter concept takes depreciation out of capital services and treats it as an intermediate input expense. The resulting net value added TFP growth will be equal to a magnification factor times the corresponding traditional value added TFP growth and the magnification factor will be approximately equal to the reciprocal of the share of labour and waiting services in traditional labour and capital services (which include depreciation in the user costs of capital). In some regulatory contexts, we may want to compute TFP growth with labour added regarded as an intermediate input and only capital services in the primary input base and compare this TFP growth with more traditional measures. Again a magnification factor will emerge. Generally speaking, the smaller we make the input base in the productivity measure, the larger will be the rate of TFP growth. Calver (2015) has provided an empirical illustration of this relationship for Australian industries. Other examples of this magnification effect can be found in Schreyer (2001) and Balk (2009).

References

21 For applications of this net value added approach and estimates of the resulting magnification factors, see Diewert (2014) and Diewert and Yu (2012).
22 For an application of this approach, see Lawrence, Diewert and Fox (2006).